

# Practice on Estimating Beta & Mmax

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# Motivation

## ❖ Target Parameters: Beta & Mmax

- Gutenberg-Richter relation

$$\log N = a - bM \text{ or } \ln N = \alpha - \beta M$$

- P.d.f. of magnitude: doubly truncated exponential function

$$f(m) = k\beta e^{-\beta(m-m_0)},$$

$$\text{where } k = [1 - e^{-\beta(m_1-m_0)}]^{-1}, m_1 = m_{max}, m_0 = m_{min}$$

## ❖ Inter-linkage of Beta & Mmax

- They are linked each other, if  $m_{max}$  is to be estimated by using
  - Seismic catalog
  - Doubly truncated exponential function
- **Estimating one needs information of the other**

# Data Preparation

## ❖ Monte-Carlo Simulation

- $M_{\min}=3.0$ ,  $M_{\max}=7.0$
- $b=1.0 \rightarrow \beta=2.306\dots$

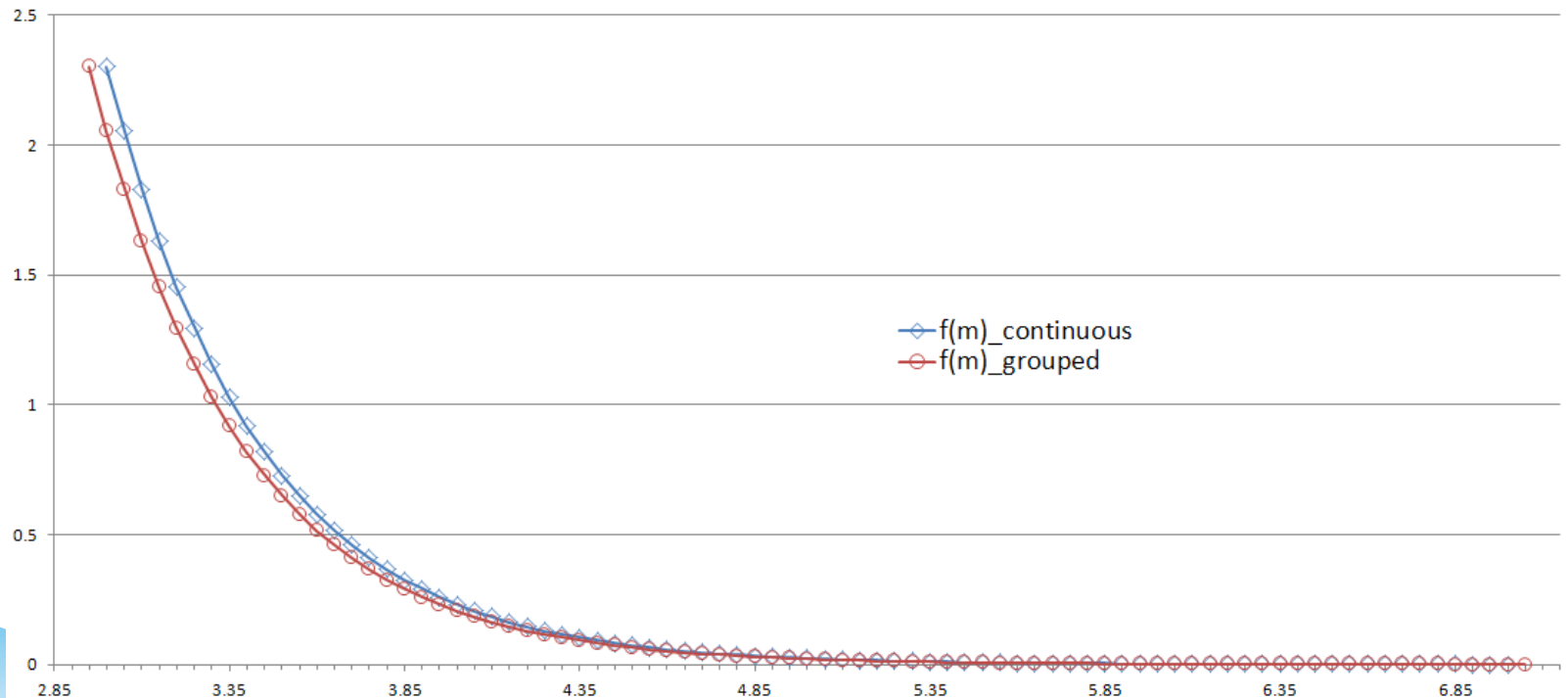
## ❖ Sample Sizes

- For seismic catalogs of 100 ~ 1,500 events
  - Estimate  $\beta$  and  $M_{\max}$  for every 100 events
- For seismic catalogs of 2,000 ~ 15,000 events
  - Estimate  $\beta$  and  $M_{\max}$  for every 1,000 events

# Data Preparation

## ❖ Adjustment for Magnitude Grouping

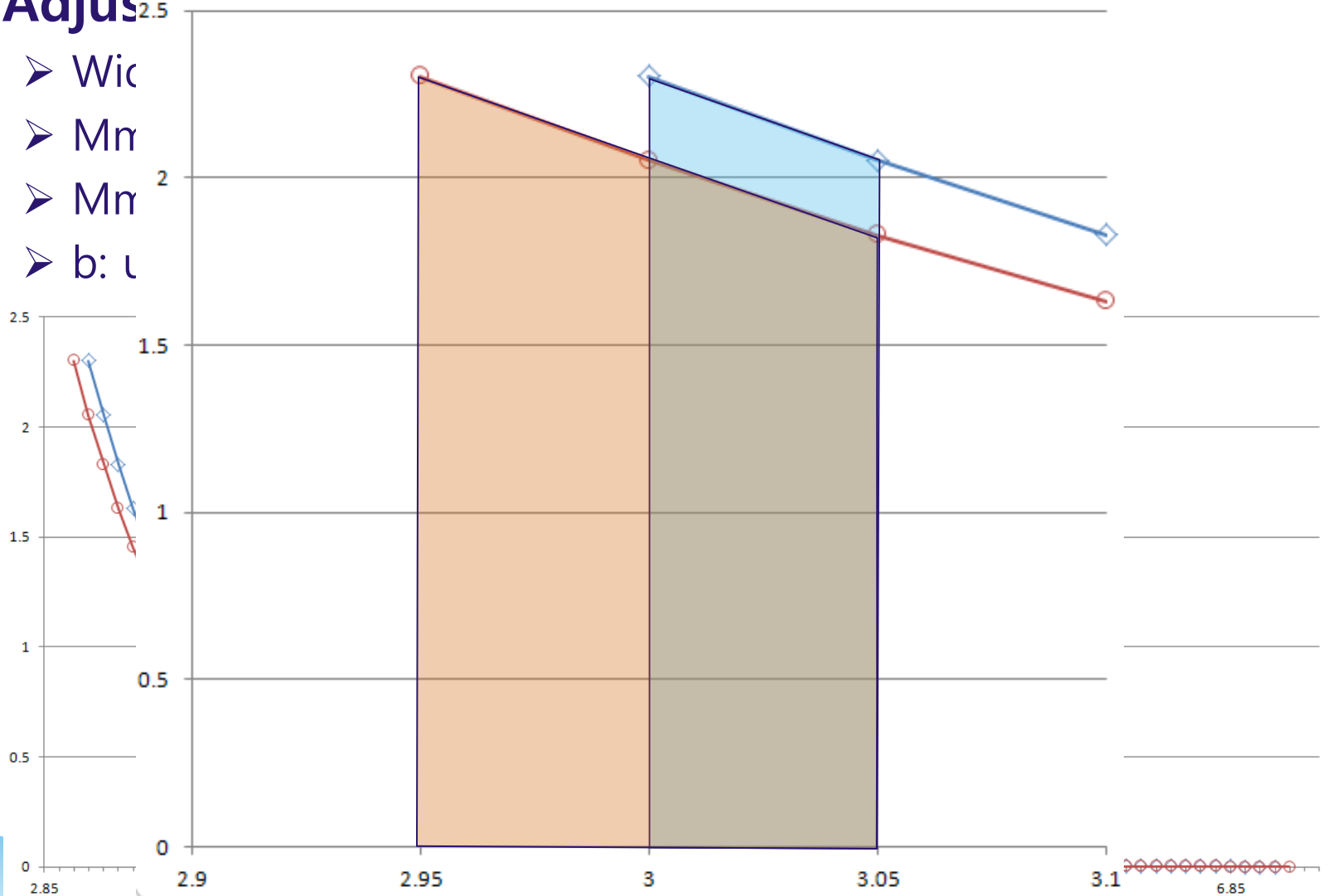
- Width of magnitude interval:  $\Delta M=0.1$
- $M_{\min} \rightarrow M_{\min}-\Delta M/2 = 2.95$
- $M_{\max} \rightarrow M_{\max}+\Delta M/2 = 7.05$
- $b$ : unchanged



# Data Preparation

## ❖ Adjustment for Magnitude Grouping

- $W_{ic}$
- $M_{nr}$
- $M_{nr}$
- $b: u$



# Estimation Methods

## ❖ Estimating Beta: Weichert (1980, BSSA)

- An equal observation period
- $\Delta M = 0.1$

## ❖ Estimating Mmax: Case I of Kijko (2004, P&A Geophy.)

- Truncated exponential distribution assumed

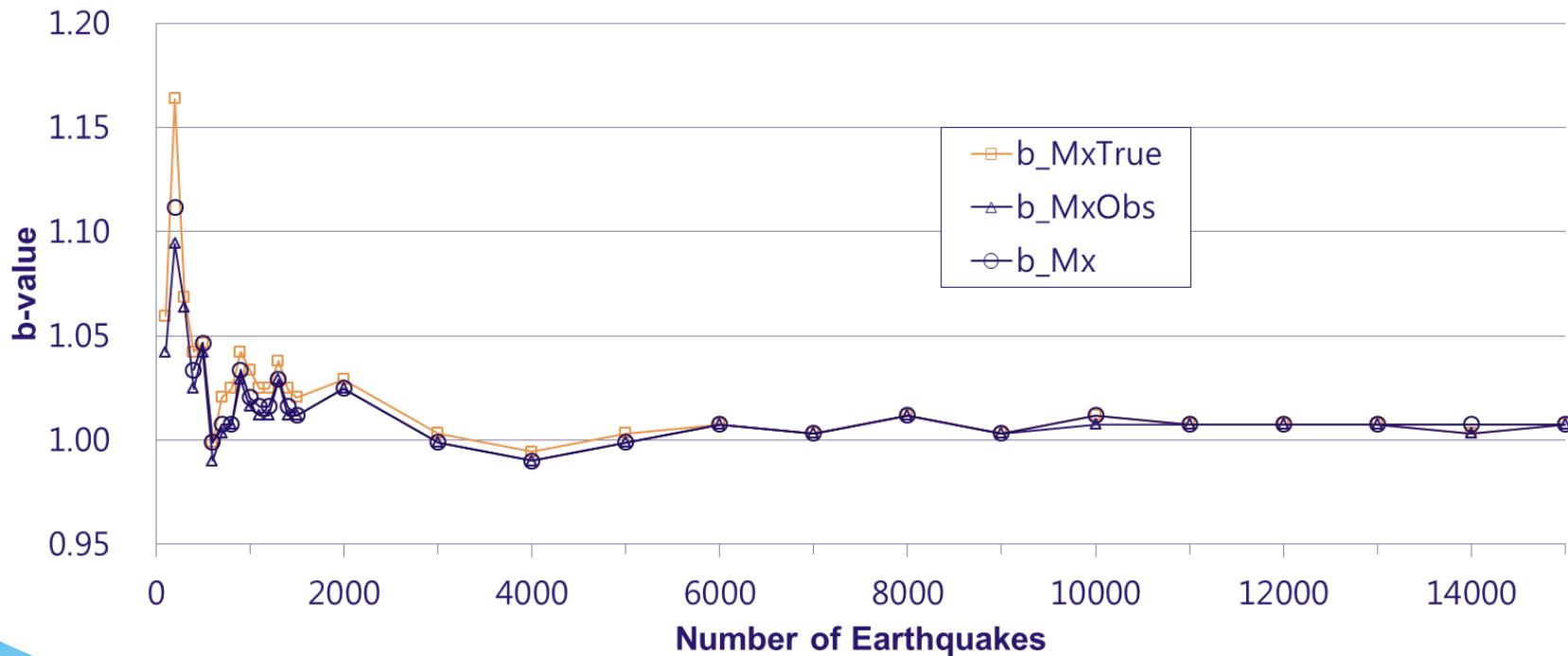
## ❖ Combined Estimation of Beta & Mmax

- Iterated estimation starting with estimating beta
  - Observed Mmax as an initial guess
- Estimating methods are the same as above

# Results

## ❖ Estimating Beta

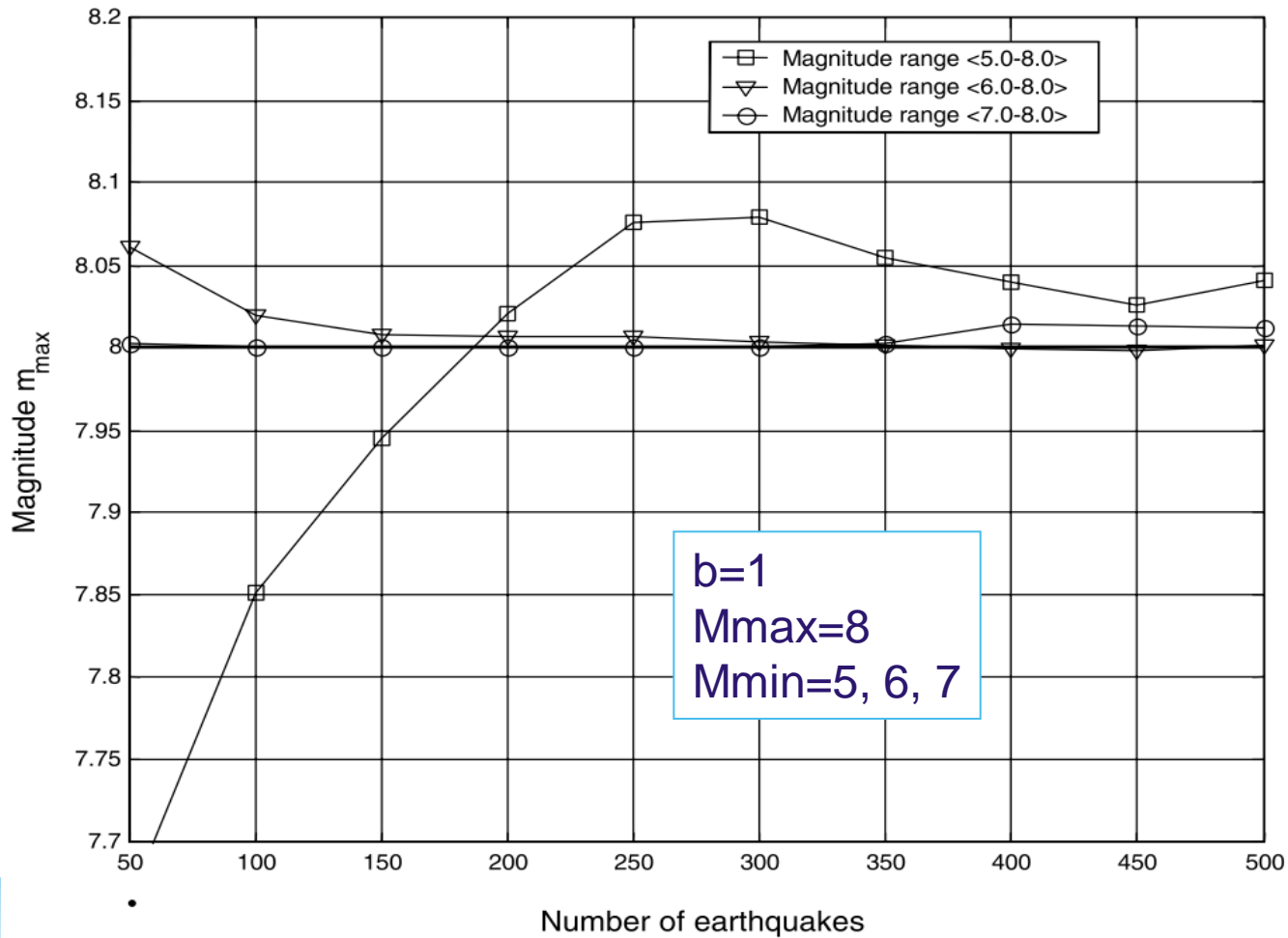
- Effect of  $M_{max}^{true}$  is insignificant
  - Use of  $M_{max}^{obs}$  yields a beta estimate accurate enough
- Beta estimation is stable for small sample size, i.e. 1000 events





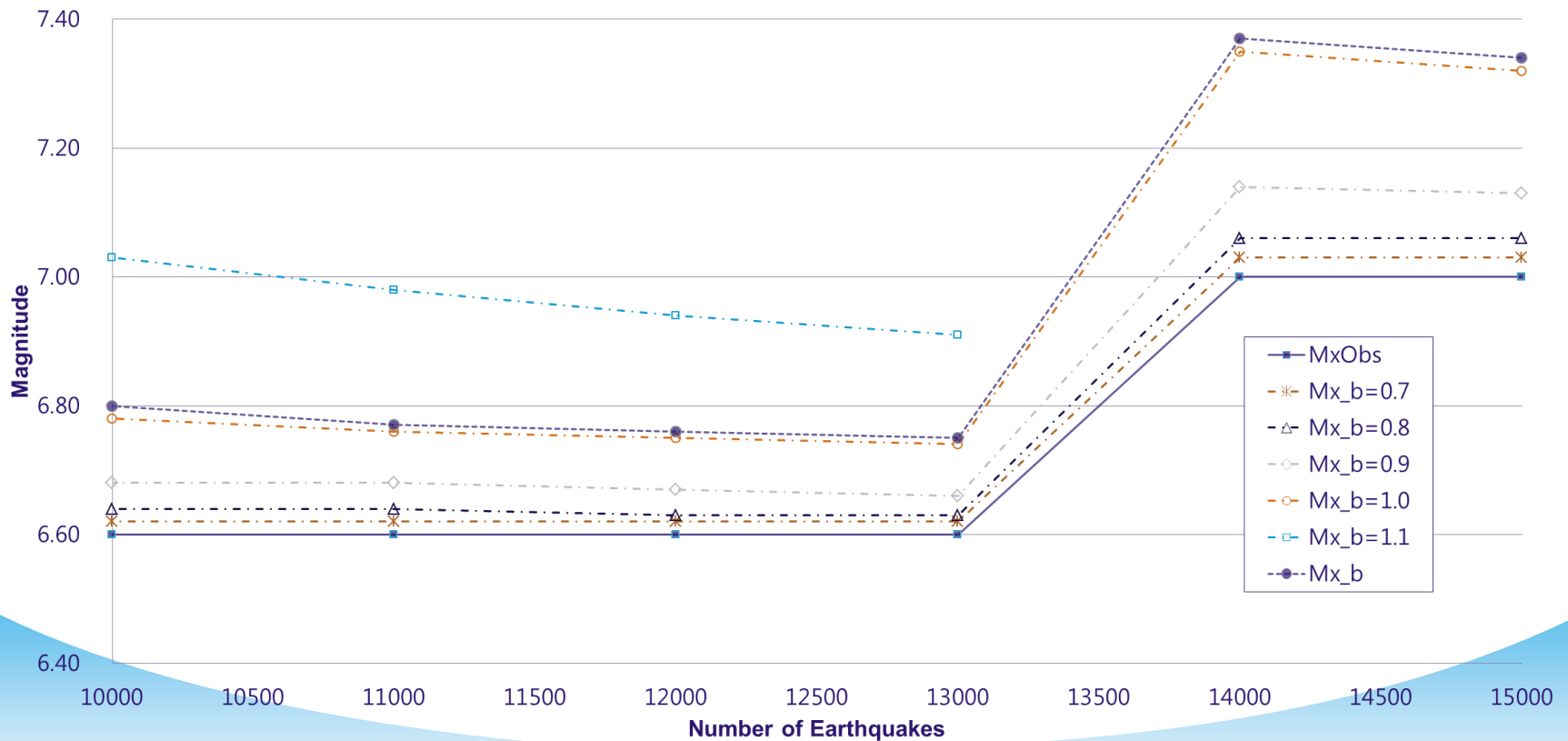
## ❖ Estimating Mmax

- Effect of sample size (Kijko, 2004, P&A Geophy.)



## ❖ Estimating Mmax (continued)

- It is significantly dependent on BETA values
- Combined estimation yields reasonable estimates
- Mmax is over-estimated, if  $M_{max}^{obs} = M_{max}^{true}$  (= Mmax)



# Summary

- ❖ **Estimate Beta first,**
  - $M_{max}^{obs}$  can effectively replace the unknown  $M_{max}^{true}$
- ❖ **Then Estimate Mmax**
- ❖ **Better Estimate by Iterative scheme**
  - Starting with beta estimation first

# Thank You!